

# 3.1 Geometry corrections – Efficiency Transfer





#### Moens theorem

- Virtual peak-to-total ratio independent of the sample for a given gamma-ray energy
- Virtual efficiencies do not take scattering into account
- Virtual peak efficiency equivalent to the usual full-energy-peak efficiency
- Virtual total efficiency can only be calculated (except for a point source)
- $\square$  P<sub>1</sub>/T<sub>1</sub> = P<sub>2</sub>/T<sub>2</sub> for two different samples 1 and 2



### Moens theorem

#### $\square P/T = (\tau + \kappa \sigma)/\mu$

- $\tau$  = photo-effect absorption coefficient
- $\sigma$  = Compton absorption coefficient
- $\mu$  = Total absorption coefficient
- $\kappa \kappa$  = percentage of Compton scattered gamma-rays which eventually end up in the full-energy peak (do not escape)
- $\square$   $\kappa$  can be shown to be independent of the source position
- T.Vidmar, A. Likar On the invariability of the total-to-peakratio in gamma-ray spectrometry. Applied Radiation and Isotopes 60 (2004) 191–195
- □ Moens theorem not valid for planar detectors!



### The Method

- **D**  $P_2 = P_1 (T_2/T_1)$
- $\square$  P<sub>1</sub> measured, Reference sample (calibrated standard)
- $\Box$  T<sub>2</sub> and T<sub>1</sub> calculated
- $\square$  P<sub>2</sub> efficiency for the desired (analyzed) sample
- □ In the calculated ratio  $(T_2/T_1)$  many inaccuracies of the detector model cancel out!
- Detector data can be taken from the manufacturers sheet
- □ Simultaneous "correction" for geometry and self absorption
- □ Alternative:  $P_2 = P_1 (\epsilon_2 / \epsilon_1)$ 
  - $ε_2$ ,  $ε_1$  full-energy-peak efficiencies → Monte Carlo simulation





#### The Method



Absorption:  $F = \exp(-\mu_s s) \exp(-\mu_w w) \dots$ Interaction:  $R = 1 - \exp(-\mu_{Ge}L)$ **Registration:**  $p_i = F_i R_i$ Efficiency:  $T = (1/N) \sum p_i$ 



### Study

- M-C. Lepy et al., EUROMET Action 428: Transfer of Ge detector efficiency calibration from point source geometry to other sources
- Various approaches
  - Direct Monte Carlo with and without optimization
  - Efficiency transfer with Monte Carlo efficiencies
  - Efficiency transfer with the Moens method
  - Semi-empirical methods
- Point-to-point, point-to-extended and extended-to-extended source transfers
- Efficiency transfer found to be much more consistent and reliable than direct calculation
- **Transfer with peak efficiencies (involves Monte Carlo calculations) best**
- Accuracy sufficient for environmental measurements, especially for selfabsorption correction



## The Originators

- Moens, L., De Donder, J., Xi-lei, L., De Corte, F., De Wispelaere, A., Simonits, A., Hoste, J., 1981. <u>Calculation of the</u> <u>absolute peak efficiency of gamma-ray detectors for different</u> <u>counting geometries</u>. Nuclear Instruments and Methods in Physics Research, 187, 451-472.
- Point-source reference measurements
- Sensitivity study
  - Method very sensitive to the detector diameter!
  - Otherwise quite robust
  - Sensitivity increases with decreasing energy